

# HONORS ALGEBRA 2 SUMMER PACKET 2019-2020

Your name: \_\_\_\_\_

Honors Algebra 2 is a very fast paced and rigorous course. The topics in this packet are considered prerequisite skills. It is imperative that you are comfortable with all of these types of problems before the first day of class. We are assigning this packet to give everyone a refresher on the skills they need to be successful in a challenging course.

In general, you must know how to do all these problems WITHOUT a calculator. You should also know the difference between a rounded value and an exact value. **All answers in this packet and in the course should be answered exactly.** For example you should write  $\pi$ , not 3.14,  $1/3$  not .3333 and  $\sqrt{5}$ , not 2.236. **All fractions and radicals should be in simplest form and should be left as improper fractions, not mixed fractions.**

**Rules for the packet:** You may collaborate with others, look things up on google, consult old notes, textbooks, etc., but all of your work on this packet must be your own. You know the difference between working together and copying. Do your own work!

## **How will this packet be graded?**

- You will have an assessment on the concepts included in these problems at the end of the first week of school. **This is considered a summative assessment of prerequisite skills and may NOT be retaken.**
- The packet is DUE on the FIRST DAY of school. It will be counted as a homework grade.

**Don't be like this comic!**



## Important Concepts, Formulas, and Notation

### Slope Formula

$$\frac{\text{rise}}{\text{run}} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$$

### Equations of Lines

Slope-Intercept Form:	$y = mx + b$
Point-Slope Form:	$y - y_1 = m(x - x_1)$
Standard Form:	$Ax + By = C$

**Exponential Function**  $y = a \cdot b^x$

### Forms of quadratic functions

Vertex Form:	$f(x) = a(x - h)^2 + k$
Standard Form:	$f(x) = ax^2 + bx + c$
Factored Form:	$f(x) = (x - d)(x - e)$

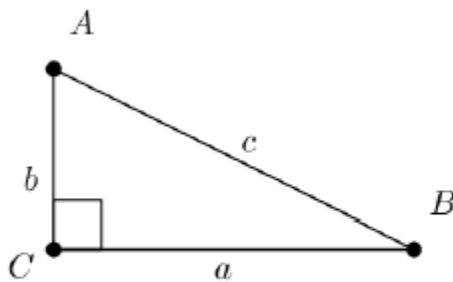
**Quadratic Formula:** If  $ax^2 + bx + c = 0$ , then  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ .

**Zero-product property:** If  $a \cdot b = 0$ , then  $a = 0$  or  $b = 0$ .

### Pythagorean Theorem:

In a triangle with sides  $a$ ,  $b$ , and longest side  $c$ , the equation  $a^2 + b^2 = c^2$  holds if and only if the triangle is a right triangle.

### Right triangles



$$\sin A = \frac{a}{c} = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\cos A = \frac{b}{c} = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan A = \frac{a}{b} = \frac{\text{opposite}}{\text{adjacent}}$$

$$c^2 = a^2 + b^2$$

Order of Operations

<https://www.youtube.com/watch?v=ipCPalumKJc>

Operations with Fractions

<https://www.youtube.com/watch?v=xLHC23-6Fz4>

Evaluating Expressions

<https://www.youtube.com/watch?v=YA9qEHnsdvQ>

Solving Multistep equations

<https://www.youtube.com/watch?v=Rqac2XAk1oA>

<https://www.youtube.com/watch?v=XIbDvq5zcys>

Solving Systems of Equations

<https://www.youtube.com/watch?v=HvPbGgvTbQs>

Graphing Linear Equations

<https://www.youtube.com/watch?v=nojSLJ9KYvQ>

Simplifying Expressions with Exponents

<https://www.youtube.com/watch?v=LMDHi935XAQ>

Factoring Polynomials

[https://www.youtube.com/watch?v=SAwE\\_fszXhQ](https://www.youtube.com/watch?v=SAwE_fszXhQ)

<https://www.youtube.com/watch?v=glc1steY5a8>

<https://www.youtube.com/watch?v=zgiXb7bgY6A>

Solving Quadratics Zero Product Property

<https://www.youtube.com/watch?v=dwCpQm9k2VI>

Solving Quadratics Quadratic Formula

<https://www.youtube.com/watch?v=S0XXBaECixo>

Trigonometry and Pythagorean Theorem

<https://www.youtube.com/watch?v=Jsiy4TxgIME>

<https://www.youtube.com/watch?v=AA6RfgP-AHU>

## Order of Operations

Simplify each expression.

a.  $\frac{8}{5-1}(3-6)^2(4)$

b.  $12 \div 2(4+3)$

c.  $16 \div 2[8-3(4-2)]+1$

d.  $\frac{2}{3} + \frac{1}{12} =$

e.  $\frac{3}{7} - \frac{1}{2} =$

f.  $\frac{2}{3} \left(\frac{27}{5}\right) =$

g.  $\frac{7}{9} \div \frac{1}{3} =$

h.  $-\frac{3}{2} + \frac{5}{4} - \frac{5}{6}$

i.  $\frac{4}{3} - \frac{6}{5} + \frac{9}{10}$

j.  $\frac{1}{5} - \frac{2}{5} \cdot \frac{15}{8}$

k.  $\frac{2}{3} + \frac{7}{12} \div \frac{21}{4}$

## Evaluating Expressions

Evaluate each expression.

a)  $2x^3 + 3x^2 - 5x$  when  $x = -3$

b)  $-d^2 - 16d - 12$  when  $d = 2$

c)  $h(n) = \frac{4}{3}n + \frac{8}{5}$ ; Find  $h(-1)$

d)  $f(x) = -1 + \frac{1}{4}x$ ; Find  $f\left(\frac{3}{4}\right)$

e)  $f(2) \cdot f(-2) + f(3)$  for the function  $f(x) = x^2 + 6x - 13$

## Solving Equations

Solve each equation for x.

a)  $-4(3 - x) = 2(x - 6)$

b)  $2(4x + 6) + 8 = 6x$

c)  $3x - 2(x + 1) = 0$

d)  $6(x + 2) + 1 = 2(x + 4)$

e)  $7x = 4x - 2$

f)  $7x + 19 = 55 - 2x$

g)  $2x + 7 + x = 4(x + 2) - 5$

h)  $4(1 - x) + 3x = -2(x + 1)$

# Systems of Equations

Solve each system using the indicated method. Check your solution.

a.) linear combination

$$5x + 4y = 6$$

$$-2x - 3y = -1$$

b.) substitution

$$-2x + y = 8$$

$$y = -3x - 2$$

c.) any method

$$3x - 2y = 5$$

$$-6x + 4y = 7$$

d.) any method

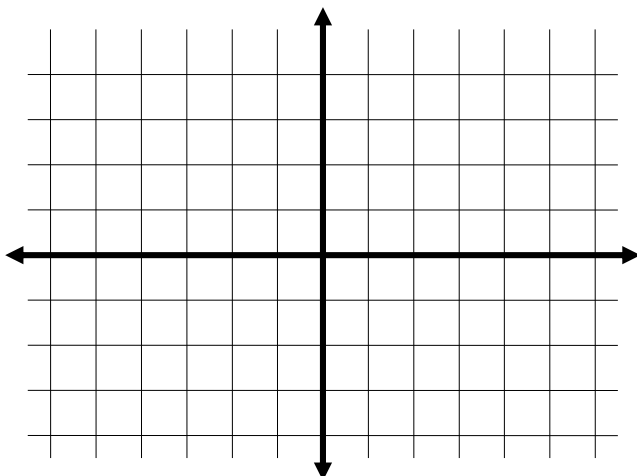
$$-x + 2y = 11$$

$$3x - 2y = -13$$

# Linear Equations

Given  $2x - 3y = -6$

a) Graph the equation.

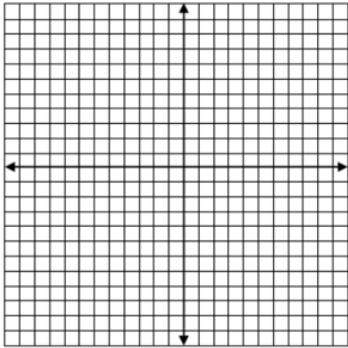


b) Determine the slope and y-intercept.

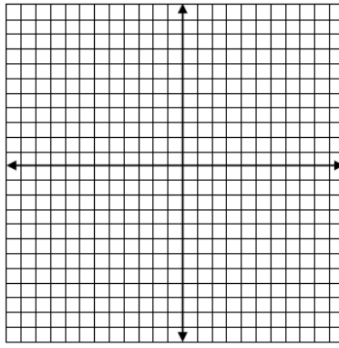
c) Select two points on the line and use them to confirm, algebraically, that the slope you calculated from part (b) is correct.

Graph each equation.

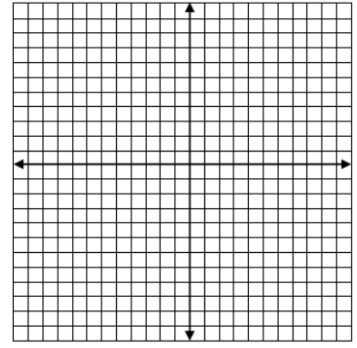
d)  $y = 3x - 1$



e)  $y = 2$



f)  $x = -1$



## Exponents Properties

Simplify each expression using only positive exponents.

### Properties of exponents

$$a^m \cdot a^n = a^{m+n} \quad (a^m)^n = a^{mn} \quad a^0 = 1$$

$$(ab)^m = a^m b^m \quad a^{-n} = \frac{1}{a^n}$$

$$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m} \quad \frac{a^m}{a^n} = a^{m-n}$$

a)  $x^3 \cdot x^5$

b)  $(x^4)^6$

c)  $\frac{x^7}{x^2}$

d)  $\left(\frac{3x}{y}\right)^2$

e)  $x^{-2} \cdot x^{-4} \cdot x^6$

f)  $(x^2 y z^3)^4$

g)  $\frac{a^2 b^{-3}}{a^{-4} b^5}$

h)  $\left(\frac{x^{-2}}{y^3}\right)^3$

i)  $(5x^{-3} y^2)^{-2}$

## Factoring

Factor each expression. Check your answer by multiplying the factored form back into standard form.

a)  $x^2 - 3x + 10$

b)  $3x^2 - 6x$

c)  $x^2 - 81$

d)  $2x^2 - 7x - 4$

e)  $x^2 - x - 72$

f)  $7x^3 - 12x^2 - 4x$

g)  $2a^2 - 11a + 15$

h)  $4r^2 - 81$

i)  $3d^2 - 16d - 12$

## Solving Quadratics

Solve each equation by factoring. Check your solution.

**a)**  $x^2 - 2x - 3 = 0$

**b)**  $x^2 - 16 = 0$

**c)**  $x^2 + 4x = 0$

**d)**  $x^2 - 6x + 9 = 0$

**e)**  $x^2 + 3x - 10 = 0$

**f)**  $5x^2 + 5x - 10 = 0$



**g)**  $3a^2 - 2a - 5 = 0$

**h)**  $2n^2 + 3n - 9 = 0$

**i)**  $3x^2 - 8x = -4$

Solve each equation using the Quadratic Formula.

**a)**  $x^2 + 5x - 1 = 0$  **b)**  $x^2 + 10x = 9$  **c)**  $x^2 - x - 1 = 0$

**d)**  $2x^2 + 3x = -8$

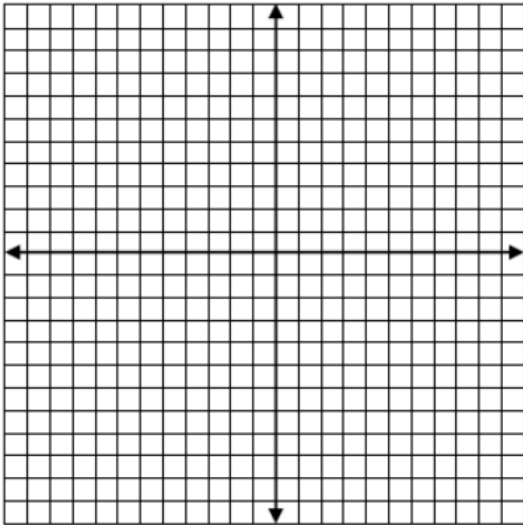
**e)**  $-2x^2 + 3x + 2 = 0$

**f)**  $x^2 - 5 = 3x - 1$

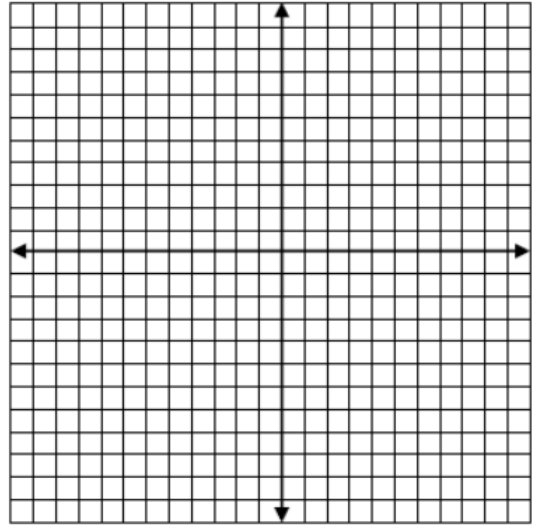
## Graphing Quadratics

Graph each equation accurately using at least 3 points.

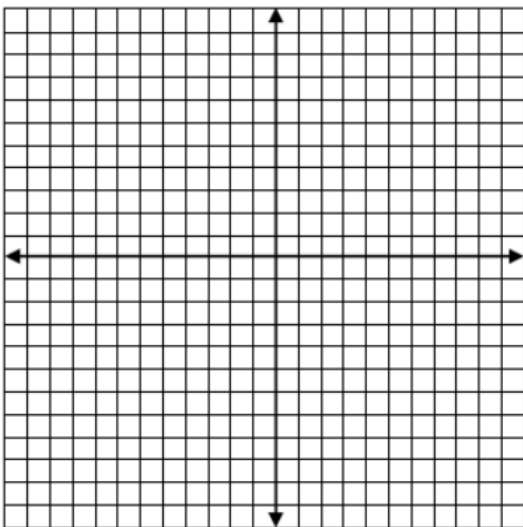
**a)**  $f(x) = x^2 - 4x + 7$



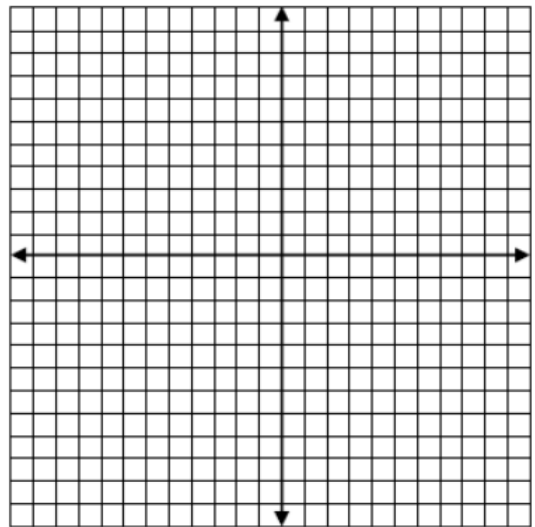
**b)**  $y = -x^2 - 6x - 10$



**c)**  $f(x) = (x + 2)^2 - 1$



**d)**  $f(x) = -2(x + 5)^2 - 3$



# Trigonometry

Find the following...

Leg opposite  $\angle A$

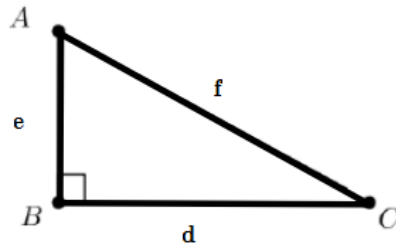
Cosine of ratio  $\angle A$

Leg opposite  $\angle C$

Tangent ratio of  $\angle A$

Sine Ratio of  $\angle A$

Sine ratio of  $\angle C$



What is the...

The angle whose Tangent ratio is  $\frac{d}{e}$

The angle whose Sine ratio is  $\frac{e}{f}$

Find the missing side length (if possible).

